



Co-optimization approach to post-storm recovery for interdependent power and transportation systems

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Abstract The power and transportation systems are urban interdependent critical infrastructures (CIs). During the post-disaster restoration process, transportation mobility and power restoration process are interdependent, and their functionalities significantly affect other well-beings of other urban CIs. Therefore, to enhance the resilience of urban CIs, successful recovery strategies should promote CI function cooperatively and synergistically to distribute goods and services efficiently. This paper develops an integrative framework that addresses the challenges of enhancing the recovery efficiency of urban power and transportation systems in short-term recovery period. Specifically, the post-storm recovery process is considered as a scheduling problem under the constraints representing crew dispatch, equipment and fuel limit. We propose a new framework for co-optimizing the recovery scheduling of power and transportation systems, respecting precedence requirement and network constraints. The advantages and benefits of co-optimized recovery scheduling are validated in a testing system.

Keywords Co-optimization, Interdependent critical infrastructure (CI), Power system, Resilience, Transportation system

1 Introduction

Among the most devastating natural hazards is coastal flooding caused by extreme storm events that interrupt critical infrastructures (CIs) in coastal cities, including building damage, roadway washout, power outage, gas shortage, communication disruption, etc., all of which lead to significant economic losses. For example, Hurricane Irma left around 6.2 million customers without power in Florida [1]. Flooding, debris caused numerous road closure around Northeast Florida and portions of I-4 washed out. The devastating effects of Hurricanes Harvey and Irma are estimated to cause economic loss between \$42.5 billion to \$65 billion [2].

With continuous rapid urbanization and growing population in coastal zones, anthropogenic changes make the coastal cities and coastal infrastructures more vulnerable to damage from extreme storms. Both the intensity and frequency of extreme storm events are expected to increase because of the climate change [3], and coastal flooding is expected to worsen in the future. Therefore, it is critically essential to enhance the resilience of CIs against extreme storm. In the short term, it is necessary to support emergency operations and the delivery of essential supplies. Debris on the main roadway need be cleared, then equipment and crews could be transported to restore power systems. Power restoration efforts should be steadily progressing to ensure other electricity-enable CIs are operational in the short term and intermediate term. Without electricity, providing transportation services can be a

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challenge as electricity powers the traffic signaling, switches, and gas stations. Power supply and traffic efficiency will significantly affect functions and restoration of other CI systems, such as water and communication systems. Therefore, to enhance the resilience of urban CIs, successful recovery strategies should promote interdependent critical infrastructures (ICIs) (such as roadway and power) function cooperatively and synergistically to distribute goods and services efficiently.

There is rich power literature on resilience against disaster, such as component hardening, cascading failures, resilience enhanced by microgrid, etc. For example, [4] presents some examples from different parts of the world where distributed energy resources in a microgrid were used to provide reliable electricity supply in the wake of disasters, allowing recovery and rebuilding efforts to occur with relatively greater efficiency. Reference [5] introduces strategies for microgrid operation when it becomes islanded. Other strategies for distribution system restoration are proposed in [6–12], while planning on power restoration in transmission systems are studied in [9, 13, 14]. Reference [15] reveals the need to strengthen electric infrastructure to minimize storm damage, reduce outages, and lessen restoration time with the need to mitigate excessive cost increases to electric customers. On-site generation in microgrid showed benefits of reliability during Hurricane Sandy [10]. The estimated annual cost due to weather-related outage ranges from \$18 billion to \$70 billion between 2003 and 2012 according to [12], which also describes strategies for modernizing the grid and increasing grid resilience. Reference [16] presents a detailed review for methods and tools of forecasting natural disaster related power system disturbances, hardening and pre-storm operations, and restoration models.

Transportation system provides the network to support the mobility of goods as well as personnel. In transportation engineering, many efforts have also been devoted to the research on transportation infrastructure systems in disasters [17]. Different techniques, such as analytical models, simulation and optimization models are applied for pre- and post-event assessment or management purposes [18–21]. Analytical methods are often used to analyze potential failure risks based on probabilities. Monte Carlo simulation-based methods involve a large sample of scenarios [22]. Optimization models optimize road network performance function, such as flow via pre-disaster network design or post-disaster resource allocation [23, 24].

In transportation sector, literature often emphasizes on the traffic mobility only. In the energy sector, coordinated operation of power and natural gas systems has attracted many attention due to their interdependency with the rise of natural gas-fired generators [25–27]. However, in the

context of interdependency of energy and transportation systems, which belong to two different sectors, existing literature mostly aims at the electric vehicles and charging stations that are naturally connected to distribution network [28–30]. The interdependency between energy and transportation is indeed beyond electrical vehicles, especially in the aftermath of disasters.

The main contribution of this paper is to develop an integrative framework that addresses the challenges of enhancing the recovery efficiency of urban power and transportation systems in short-term recovery period. Although the recovery activities are synergistic and interdependent in power and transportation system, challenge of interdependency is seldom addressed in the post-storm recovery literature. In this paper, the post-storm recovery process is considered as a scheduling problem with constraints representing crew dispatch, equipment and fuel limit, and other resource sharing as well as constraints representing precedence relationship among the repair tasks. We propose a new framework for co-optimizing the repair scheduling in power and transportation systems.

The paper is organized as follows. Section 2 introduces the power and transportation systems and the recovery model. Section 3 demonstrates a case study for the proposed methods. Section 4 concludes the paper.

2 Recovery model

Post-storm recovery tasks are not independent to another. Some tasks have hard precedence relationship while others might share repair resources. For example, in order to repair components in power systems, such as generators, overhead and underground cables (lines), we have to guarantee the delivery of crew, fuel, and other resources. In this section, we will develop a co-optimization model for recovery activity scheduling in power and transportation systems.

An example of interdependent power and transportation systems is shown in Fig. 1. It consists of electricity distribution system and transportation system. We consider the electricity distribution system and the city roadway system. The electricity distribution system includes nodes, distributed generators, and transformers, while the transportation system consists of traffic intersections and roadways. It presents close topology and flow interdependency among power and transportation systems as the power nodes are often co-located around traffic intersections. Specifically, the repair of the components of power grid, after the failure caused by storms, will rely on the repair resources transported via roadways; on the other hand, the repair work of electrical components indeed will have significant impacts on the traffic flow, even cause some



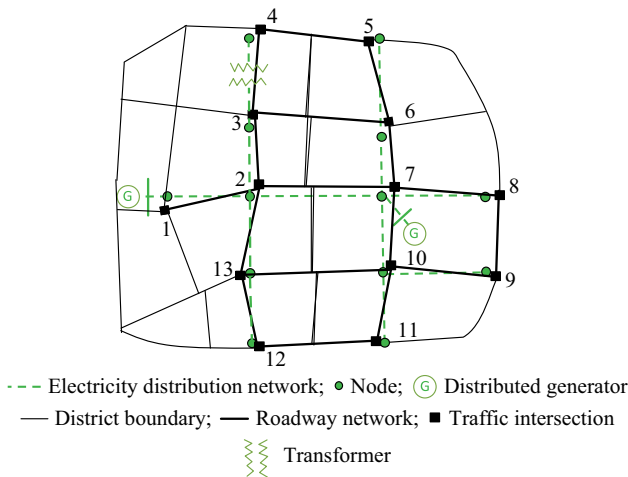


Fig. 1 An example of interdependent power and transportation systems

roadway closure. In this paper, we mainly focus on the energy recovery and road repair.

2.1 Objective of recovery

To implement the strategy discussed above, we develop a mixed-integer linear programming (MILP) model to formulate power flows, the interdependency of power and transportation systems, and crew/resource delivery. The objective is formulated as:

$$\max \left[\alpha \sum_i \sum_t D_{i,t} + (1 - \alpha) \sum_r \sum_t y_{r,t} \right] \tag{1}$$

where $D_{i,t}$ is the load in node i at time t ; $y_{r,t}$ is the indicator of road r being cleared at time t ; and α is the weight coefficient.

The objective is to restore load and clear road as much as possible. As both power and transportation systems are involved, we employ weight factor α to simplify the problem. In the extreme case, one could maximize recovered power only by setting set $\alpha = 1$.

2.2 Recovery of roadway

The crew and resources are transported to repair the blocked roadways. In this model, we consider certain amount of resources are required for clearing roads. The recovery of road is formulated as:

$$y_{r,t} \geq y_{r,t-1} \quad \forall r, t \tag{2}$$

$$\sum_{\tau=1}^t (R_{m(r),\tau} + R_{n(r),\tau}) \geq \hat{R}_r y_{r,t} \quad \forall r, t \tag{3}$$

$$y_{r,t} \in \{0, 1\} \quad \forall r, t \tag{4}$$

where $m(r)$ and $n(r)$ are the intersections connect to road r ; $R_{m(r),t}$ and $R_{n(r),t}$ are the labor resources available for road r ; and \hat{R}_r is the total labor resources needed to repair the road r .

For simplicity, the resource is assumed available for the repair once it arrives at intersection that connects to the damaged roads or is nearby out-of-service power equipment. One could always add artificial intersection near the damaged roads if accuracy is needed. Equation (2) indicates that a road is always clear once it is repaired. Equation (3) represents that the road r will be only cleared after the accumulated resources reach the required amount \hat{R}_r . Equation (4) means $y_{r,t}$ is a binary variable. The road r is clear or recovered post-storm when $y_{r,t}$ is 1, and is closed when $y_{r,t}$ is 0.

2.3 Recovery of electricity distribution line

When there are line outages in the electricity distribution system, the recovery of electricity distribution line could also be modeled via binary variables. We model the line recovery as:

$$u_{l,t} \geq u_{l,t-1} \quad \forall l, t \tag{5}$$

$$\sum_{\tau=1}^t L_{l,\tau} \geq \hat{L}_l u_{l,t} \quad \forall l, t \tag{6}$$

$$u_{l,t} \in \{0, 1\} \quad \forall l, t \tag{7}$$

where $u_{l,t}$ is the indicator of line l status; $L_{l,\tau}$ is the labor resources that used for line repair; and \hat{L}_l is the labor resources needed to repair line l .

According to (5), the line is always in normal condition once it is repaired. Equation (6) enforces the status of line l at period t . Only the labor resources that used for line repair reach the amount \hat{L}_l , line l can be back to normal operation. The line l is in normal condition or recovered at period t when $u_{l,t}$ is 1, and is not in service when it is 0.

2.4 Interdependent power and transportation systems

A key point of post-storm recovery is to consider the interdependency of the power and transportation systems. We have modeled the recovery actions for roads and cables in previous two subsections. Although both power system and transportation system are networked, the delivery mechanisms are different. More specifically, the delivery of electric power is near light-speed in electricity distribution system, while the delivery of crew and fuel via transportation sub-system has delay. Energizing components in distribution system relies on the availability of the

equipment and fuel that transported via the road network. For simplicity, the resource is assumed available for repair once it is nearby out-of-service power equipment. The model of interdependent power and transportation systems for recovery is formulated as follows.

$$R_{m,t} = R_{m,t-1} - \sum_{r \in \mathcal{F}(m)} FL_{r,t}^{R+} - \sum_{r \in \mathcal{T}(m)} FL_{r,t}^{R-} + \sum_{r \in \mathcal{T}(m)} FL_{r,t-\gamma(r)}^{R+} + \sum_{r \in \mathcal{F}(m)} FL_{r,t-\gamma(r)}^{R-} \quad \forall m, t \tag{8}$$

$$0 \leq FL_{r,t}^{R-} \leq My_{r,t} \quad \forall r, t \tag{9}$$

$$0 \leq FL_{r,t}^{R+} \leq My_{r,t} \quad \forall r, t \tag{10}$$

$$L_{m,t} = L_{m,t-1} - \sum_{r \in \mathcal{F}(m)} FL_{r,t}^{L+} - \sum_{r \in \mathcal{T}(m)} FL_{r,t}^{L-} + \sum_{r \in \mathcal{T}(m)} FL_{r,t-\gamma(r)}^{L+} + \sum_{r \in \mathcal{F}(m)} FL_{r,t-\gamma(r)}^{L-} \quad \forall m, t \tag{11}$$

$$0 \leq FL_{r,t}^{L-} \leq My_{r,t} \quad \forall r, t \tag{12}$$

$$0 \leq FL_{r,t}^{L+} \leq My_{r,t} \quad \forall r, t \tag{13}$$

$$F_{m,t} = F_{m,t-1} - \sum_{i \in \mathcal{G}(m)} \omega_i P_{i,t} - \sum_{r \in \mathcal{F}(m)} FL_{r,t}^{F+} - \sum_{r \in \mathcal{T}(m)} FL_{r,t}^{F-} + \sum_{r \in \mathcal{T}(m)} FL_{r,t-\gamma(r)}^{F+} + \sum_{r \in \mathcal{F}(m)} FL_{r,t-\gamma(r)}^{F-} \quad \forall r, t \tag{14}$$

$$0 \leq FL_{r,t}^{F-} \leq My_{r,t} \quad \forall r, t \tag{15}$$

$$0 \leq FL_{r,t}^{F+} \leq My_{r,t} \quad \forall r, t \tag{16}$$

where $FL_{r,t}^{R+}$ and $FL_{r,t}^{R-}$ are the flows of road-repair resource in positive and negative directions, respectively; $FL_{r,t}^{L+}$ and $FL_{r,t}^{L-}$ are the flows of line-repair resource in positive and negative directions, respectively; $FL_{r,t}^{F+}$ and $FL_{r,t}^{F-}$ are the flows of distributed generator fuel in positive and negative directions, respectively; $\mathcal{F}(m)$ is the set of roads whose defined source intersection is m ; $\mathcal{T}(m)$ is the set of roads whose defined destination intersection is m ; $\mathcal{G}(m)$ is the set of generators that are accessed via intersection m ; $\gamma(r)$ is the time of delivering crew/resource in road r ; $R_{m,t}$ is the road-repair resource available at intersection m ; $L_{m,t}$ is the line-repair resource available at intersection m ; $F_{m,t}$ is the fuel arrived at intersection m ; $P_{i,t}$ is the generation output of unit i ; ω is the fuel-power coefficient; and M is a big number.

The repair resource and fuel flows, i.e., $FL_{r,t}^{R+}$, $FL_{r,t}^{R-}$, $FL_{r,t}^{L+}$, $FL_{r,t}^{L-}$, $FL_{r,t}^{F+}$, and $FL_{r,t}^{F-}$ in (11)-(16), all go through the road network. Hence, transporting time for repair resource and fuel must be considered, and it is modeled in flow constraints (8), (11), and (14). We model flows in two directions separately so that the arriving time, leaving time, and transporting time could be handled independently in the networked system. Equation (8) stands for the road-repair resource available in m at period t considering the resource leaving and arriving m at t . Due to the transporting time, goods flow $FL_{r,t-\gamma(r)}^{R+}$ arriving r at t indeed left its source intersection at $t - \gamma(r)$. Hence, line-repair resource at period t is a function of line-repair resource in last period, i.e. $t - 1$, leaving resource and arriving resource at t . Similarly, the line-repair resource and fuel transportations are modeled in (11) and (14), respectively.

All goods flows are limited by road network capacity in (9), (10), (12), (13), (15), and (16). For example, if $y_{r,t}$ is 0, then (9) enforces the flow $FL_{r,t}^{R-}$ be zero at time t . In other words, if road r is not cleared, the goods cannot be transported via r . The fuel consumption is modeled in (14), i.e. generating at level of $P_{i,t}$ will consume fuel at level of $\omega P_{i,t}$. At intersection m in road network, the available fuel at t is a function of fuel level at $t - 1$, fuel consumption at t , fuel transported out from m at t , and the arriving fuel at t .

2.5 Co-optimization model for post-storm recovery

For simplicity, we use a typical DC flow to model the power flow in power system. The co-optimization model for recovery scheduling is formulated as follows.

$$\left\{ \begin{array}{l} \max \left[\alpha \sum_i \sum_t D_{i,t} + (1 - \alpha) \sum_r \sum_t y_{r,t} \right] \\ \text{s.t.} \quad (2) - (16) \\ P_{i,t} - D_{i,t} = \sum_{l \in \mathcal{L}(i)} PL_{l,t} \quad \forall i, t \\ P_{i,t} \leq P_{i,t}^{\max} \quad \forall i, t \\ D_{i,t} \leq \hat{D}_{i,t} \quad \forall i, t \\ -u_{l,t} \cdot PL_l^{\max} \leq PL_{l,t} \leq u_{l,t} \cdot PL_l^{\max} \quad \forall l, t \\ -(1 - u_{l,t})M \leq PL_{l,t} - \frac{\theta_{i,t} - \theta_{j,t}}{X_l} \leq (1 - u_{l,t})M \quad \forall l, t \\ PL_{l,t} - \frac{\theta_{i,t} - \theta_{j,t}}{X_l} \leq (1 - u_{l,t})M \quad \forall l, t \\ \theta_{1,t} = 0 \quad \forall t \end{array} \right. \tag{17}$$

where $D_{i,t}$ is the recovered load at node i at time t ; $\hat{D}_{i,t}$ is the maximal load supplied at node i ; $PL_{l,t}$ is the power flow on line l at time t ; PL_l^{\max} is the maximum power flow on line l ; X_l is the reactance of line l connecting i and j ; and θ_i is the voltage angle at node i at time t .



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